

Find the asymptotic run time for each of the algorithms below. Do as many problems as you can before class on 9/6.

```
procedure SUM( $A[1..n]$ )  
   $total \leftarrow 0$   
  for  $j \leftarrow 1..n$  do  
     $total \leftarrow total + A[j]$   
  end for  
  return  $total$   
end procedure
```

```
procedure COMBINATIONS( $n$ )  
   $n \leftarrow 0$   
  for  $i \leftarrow 1..n$  do  
    for  $j \leftarrow i + 1..n$  do  
       $n \leftarrow n + 1$   
    end for  
  end for  
end procedure
```

```
procedure EDITDISTANCE( $A[1..n], B[1..n]$ )  
  Let  $C$  be an  $(n + 1) \times (n + 1)$  matrix of all zeros  
  for  $i \leftarrow 1..n$  do  
     $C[i + 1][0] \leftarrow i$   
  end for  
  for  $j \leftarrow 1..n$  do  
     $C[0][j + 1] \leftarrow j$   
  end for  
  for  $i \leftarrow 1..n$  do  
    for  $j \leftarrow 1..n$  do  
      if  $A[i] = B[j]$  then  
         $C[i + 1][j + 1] \leftarrow \min\{A[i + 1][j] + 1, A[i][j + 1] + 1, A[i][j]\}$   
      else  
         $C[i + 1][j + 1] \leftarrow \min\{A[i + 1][j] + 1, A[i][j + 1] + 1, A[i][j] + 1\}$   
      end if  
    end for  
  end for  
  return  $C[n + 1][n + 1]$   
end procedure
```

```

procedure EUCLID( $a, b$ )
   $r \leftarrow a \bmod b$ 
  while  $r \neq 0$  do
     $a \leftarrow b$ 
     $b \leftarrow r$ 
     $r \leftarrow a \bmod b$ 
  end while
  return  $b$ 
end procedure

```

```

procedure INSERTIONSORT( $A[1..n]$ )
  for  $j \leftarrow 2..n$  do
     $key \leftarrow A[j]$ 
     $i \leftarrow j - 1$ 
    while  $i > 0$  and  $A[i] > key$  do
       $A[i + 1] \leftarrow A[i]$ 
       $i \leftarrow i - 1$ 
    end while
     $A[i + 1] \leftarrow key$ 
  end for
end procedure

```

```

procedure FIBONACCI( $n$ )
  if  $n \leq 2$  then
    return 1
  else
    return FIBONACCI( $n - 1$ ) + FIBONACCI( $n - 2$ )
  end if
end procedure

```

```

procedure MERGE( $A[1..n], B[1..m]$ )
  Let  $C$  be an array of length  $n + m$ 
   $i \leftarrow 1$ 
   $j \leftarrow 1$ 
  while  $i < n$  and  $j < m$  do
    if  $A[i] < B[j]$  then
       $C[i + j] \leftarrow A[i]$ 
       $i \leftarrow i + 1$ 
    else
       $C[i + j] \leftarrow B[j]$ 
       $j \leftarrow j + 1$ 
    end if
  end while
  while  $i < n$  do
     $C[i + j] \leftarrow A[i]$ 
     $i \leftarrow i + 1$ 
  end while
  while  $j < m$  do
     $C[i + j] \leftarrow B[j]$ 
     $j \leftarrow j + 1$ 
  end while
  return  $C$ 
end procedure

```

```

procedure MERGESORT( $A[1..n]$ )
   $m = \lfloor n/2 \rfloor$ 
   $C \leftarrow$  MERGESORT( $A[1..m]$ )
   $D \leftarrow$  MERGESORT( $A[m + 1..n]$ )
  return Merge( $C, D$ )
end procedure

```